



# Arrow and Ivy

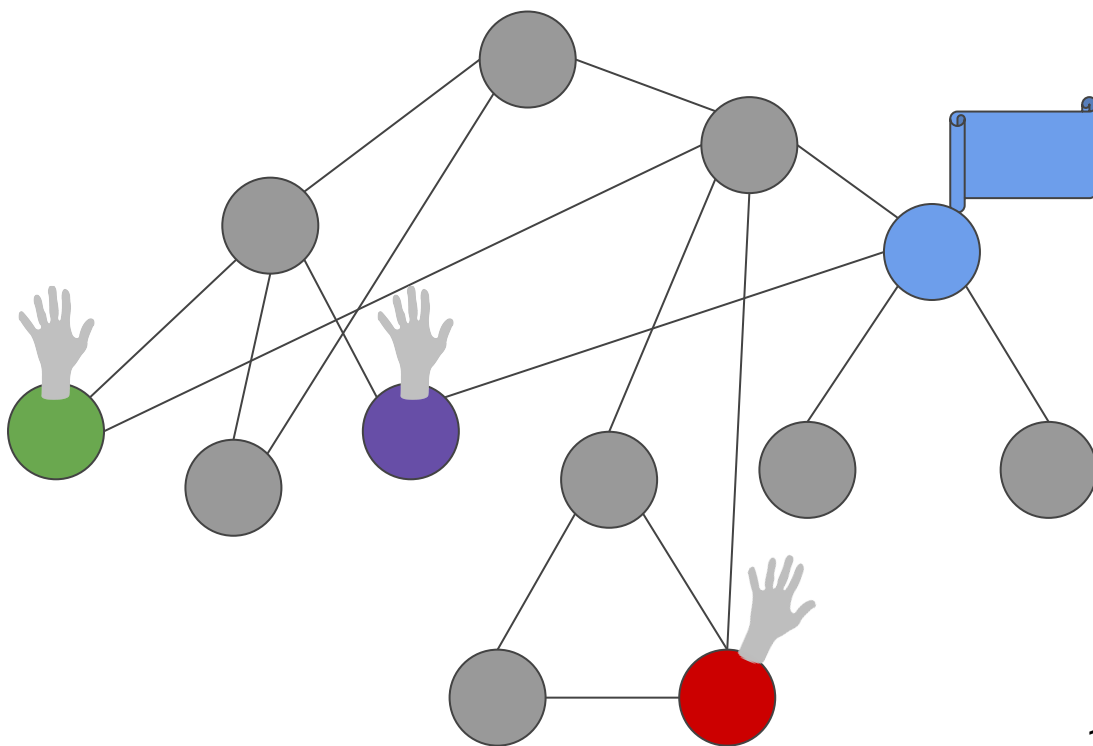
Ordering Shared Objects in Distributed Networks

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University of Vienna

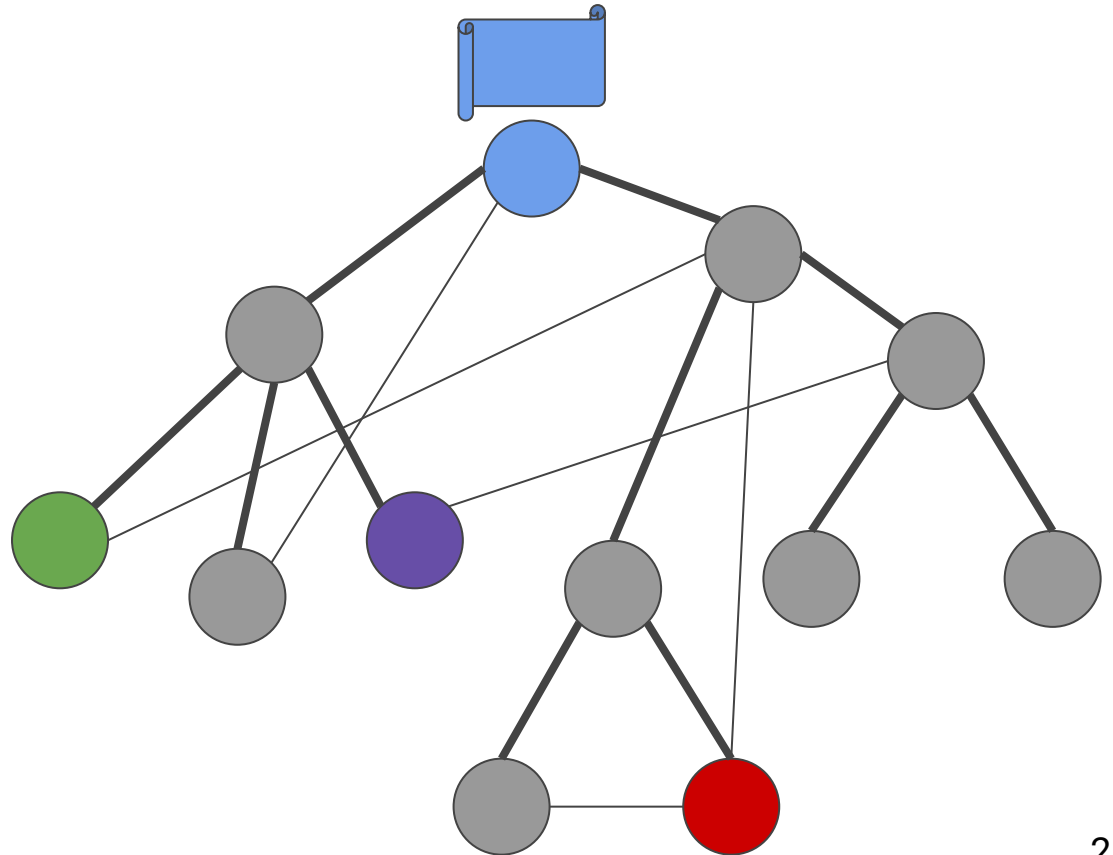
# Input

- Underlying Network
- Shared Object
  - Variable
  - Data Structure
- Requests:
  - Read
  - Write
  - Read-Modify-Write



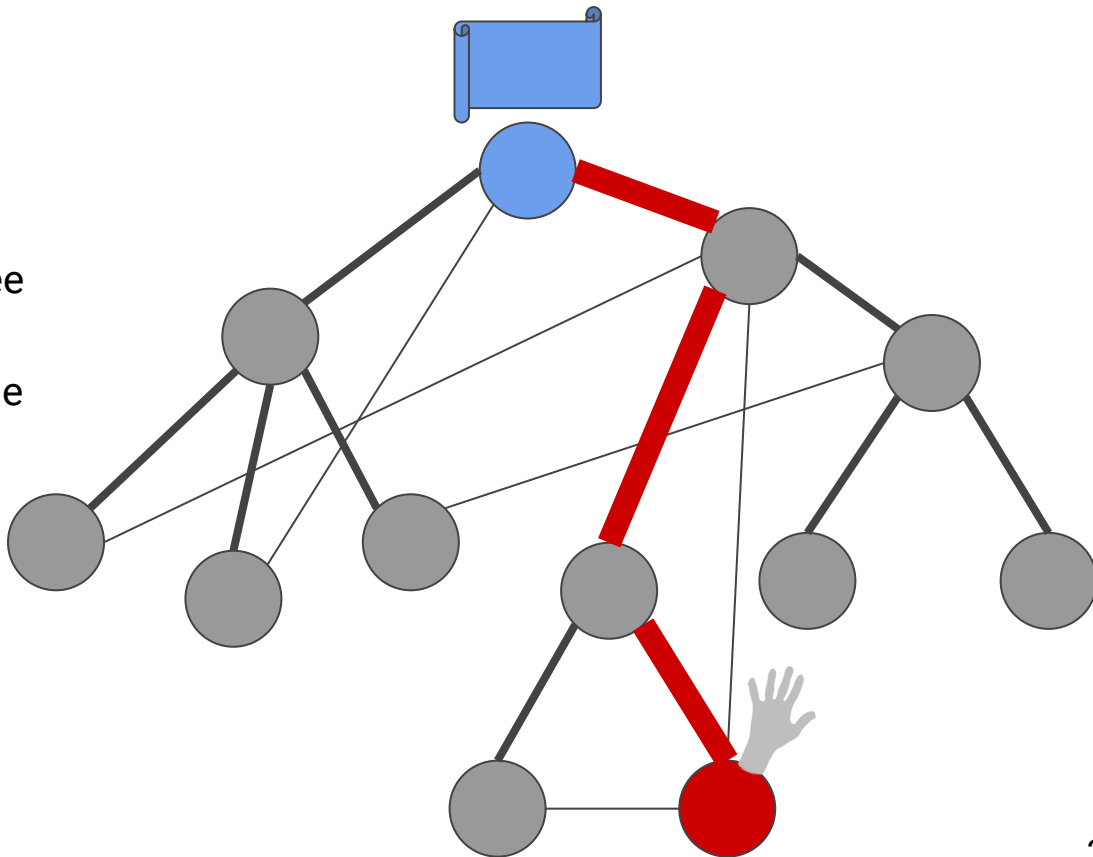
# Solutions

- Choosing a spanning Tree:
  - Optimal Choice?
  - Root
- Without Modification:
  - Central Location
  - Home Based
- With Modification:
  - Arrow
  - Ivy
  - Arvy



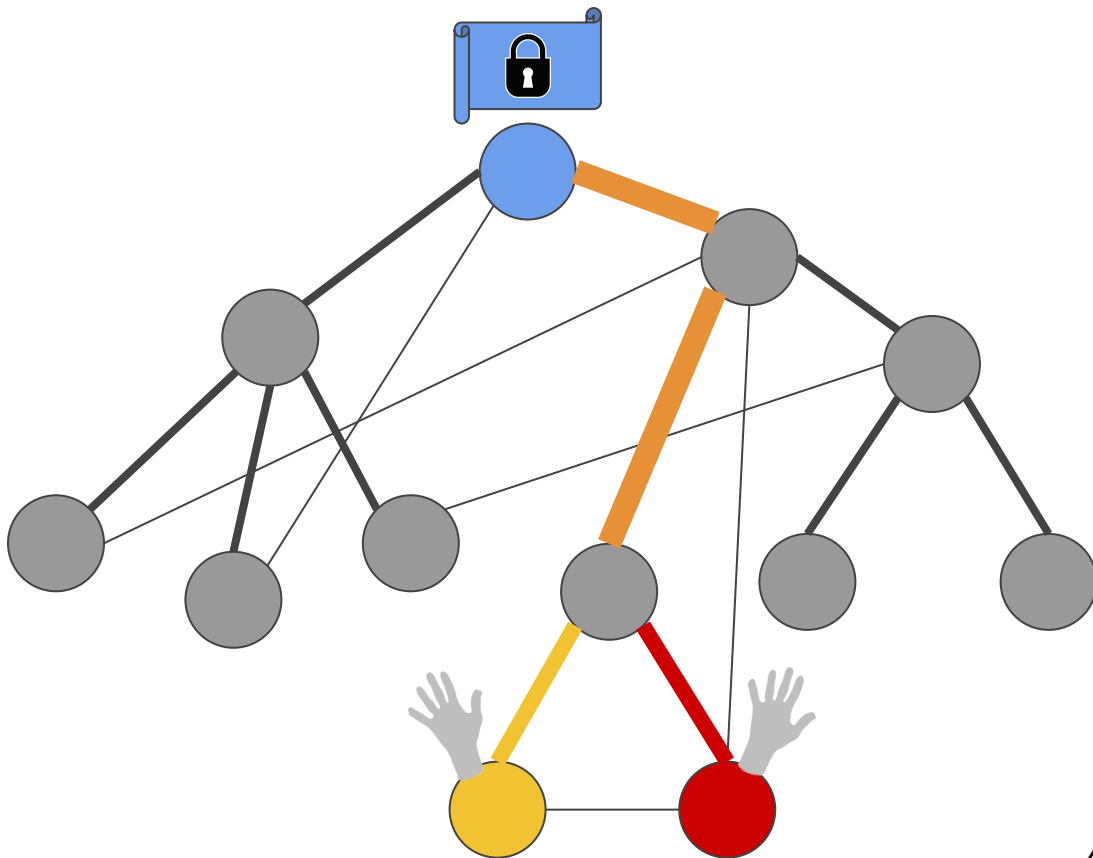
# Central Location

- Process:
  - Send requests to root
  - Root Process Requests
  - Send back result down tree
- Bad example:
  - All requests from one node
- Solutions:
  - Route back directly
  - Moving the root



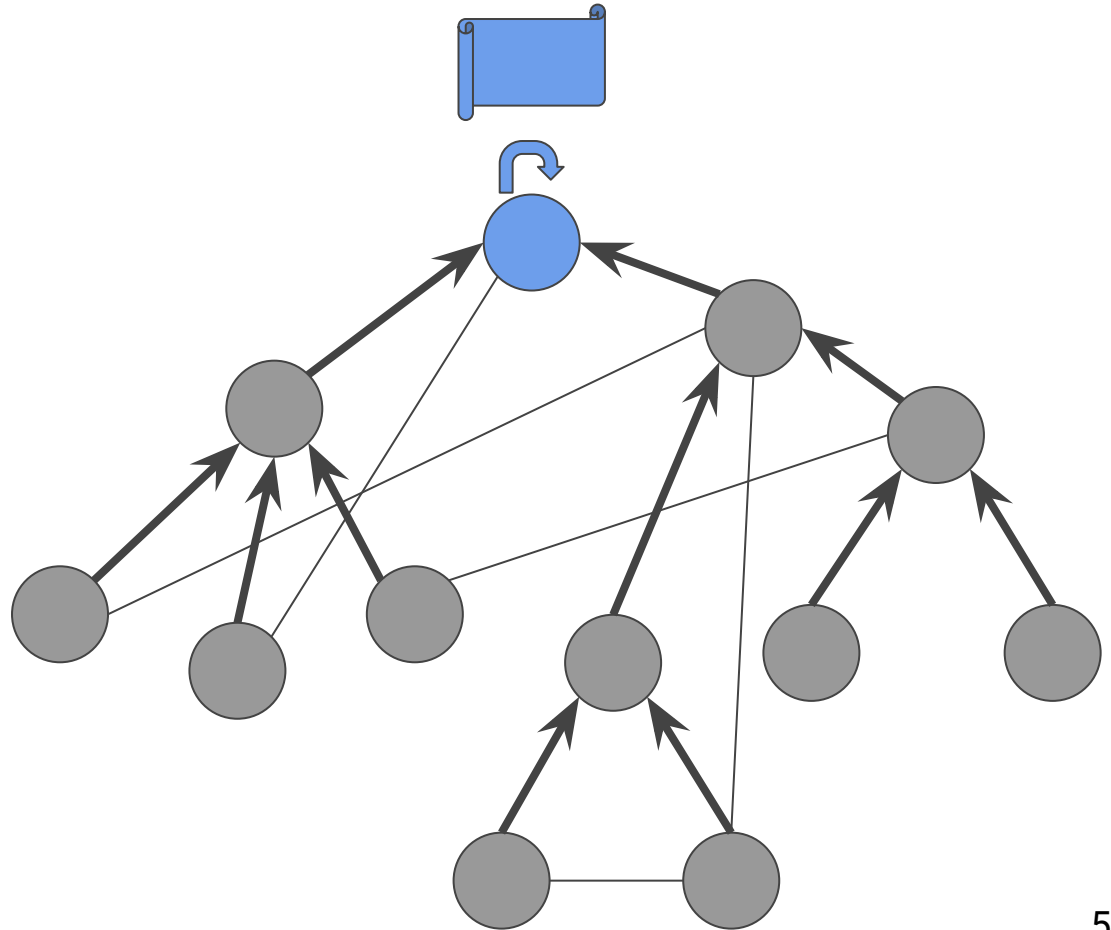
# Home-Based

- Process:
  - Known home base
  - Request a lock
  - Process Locally
- Benefits:
  - Mobile networks
- Bad example:
  - Triangle routing
- Solution:
  - Moving the root



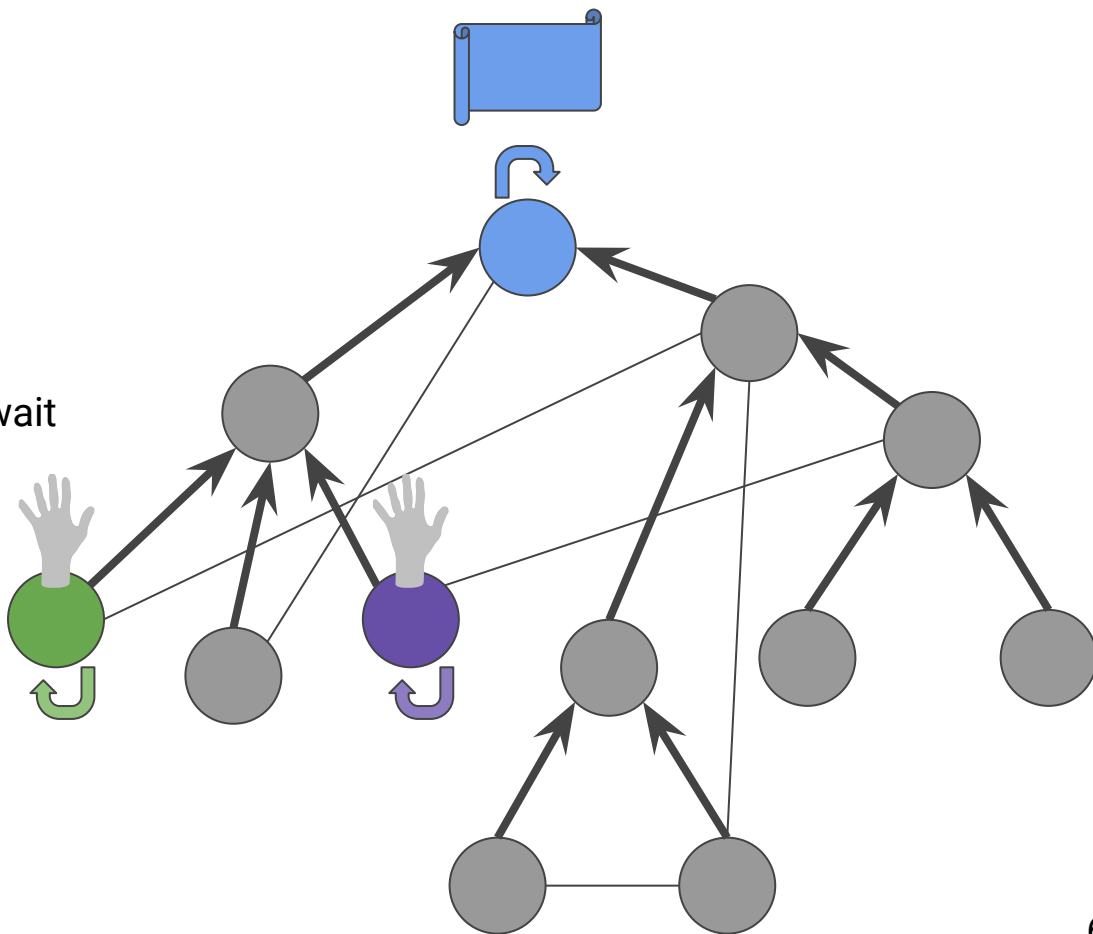
# Arrow: Protocol

- Directing tree towards root:
  - Self loop for root
  - Keep underlying graph



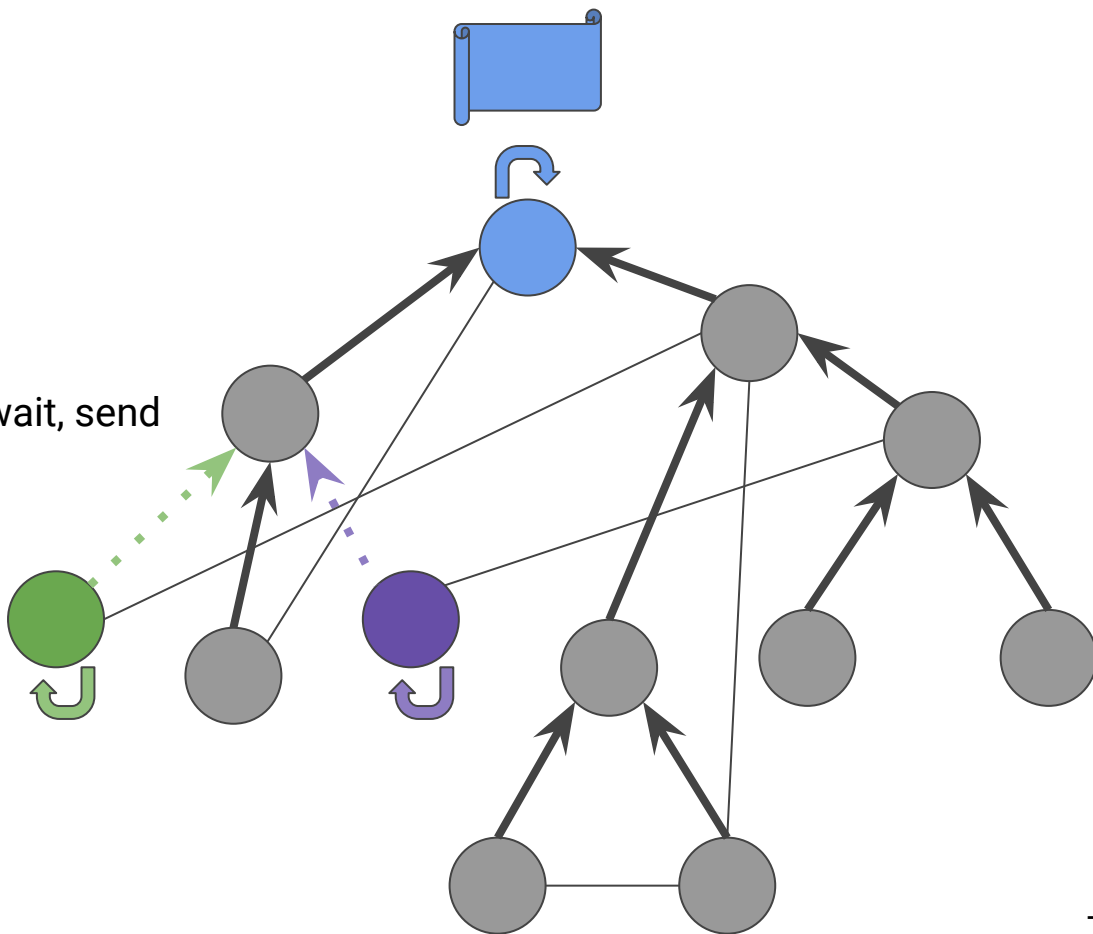
# Arrow: Protocol

- Directing tree towards root:
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- Finding process:
  - Initiator: Make Self-loop, wait



# Arrow: Protocol

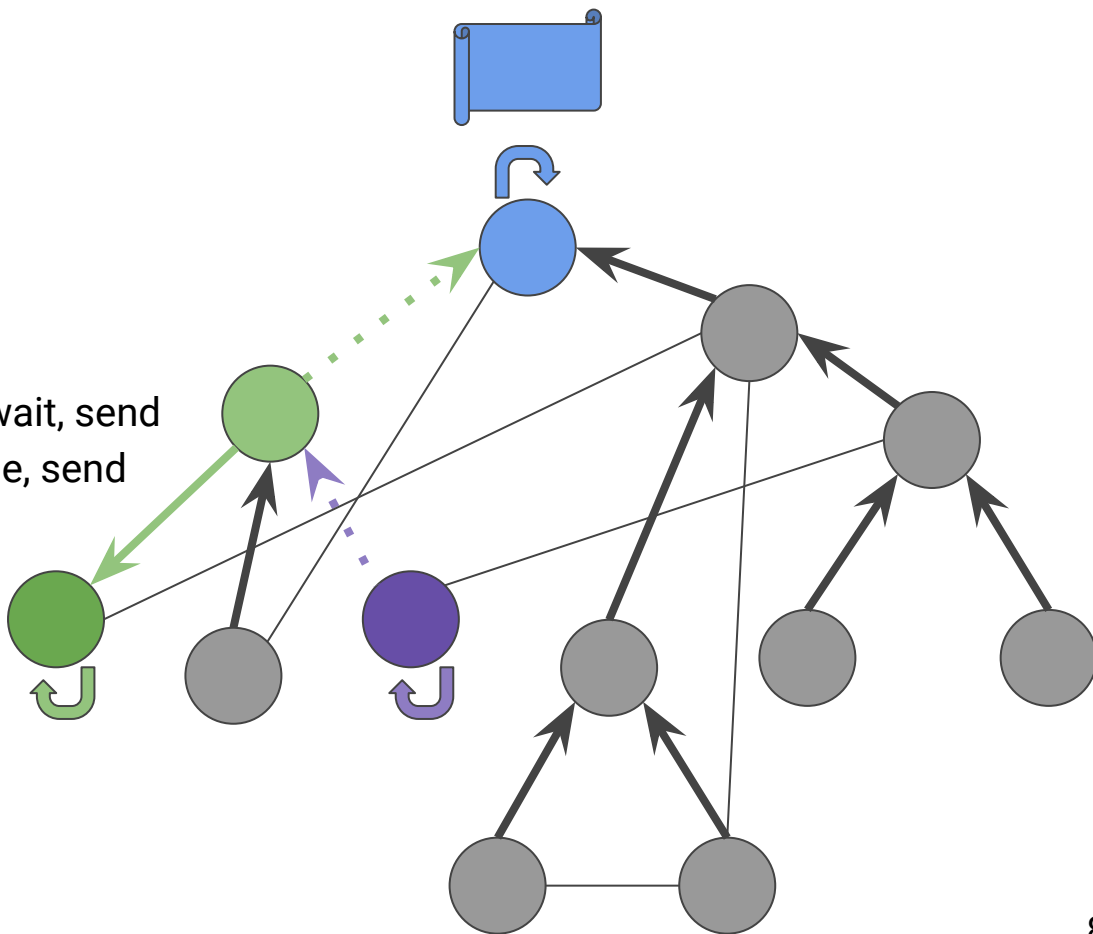
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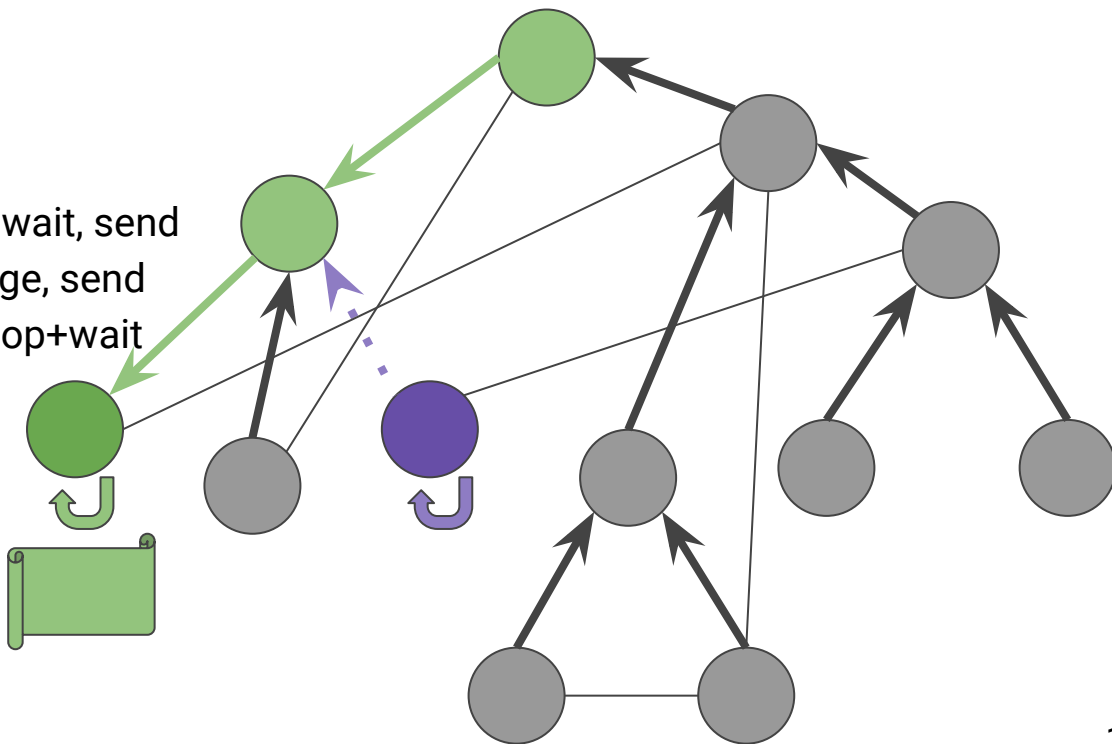
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- Directing tree towards root:
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  - Arrival: reverse arrival edge, send



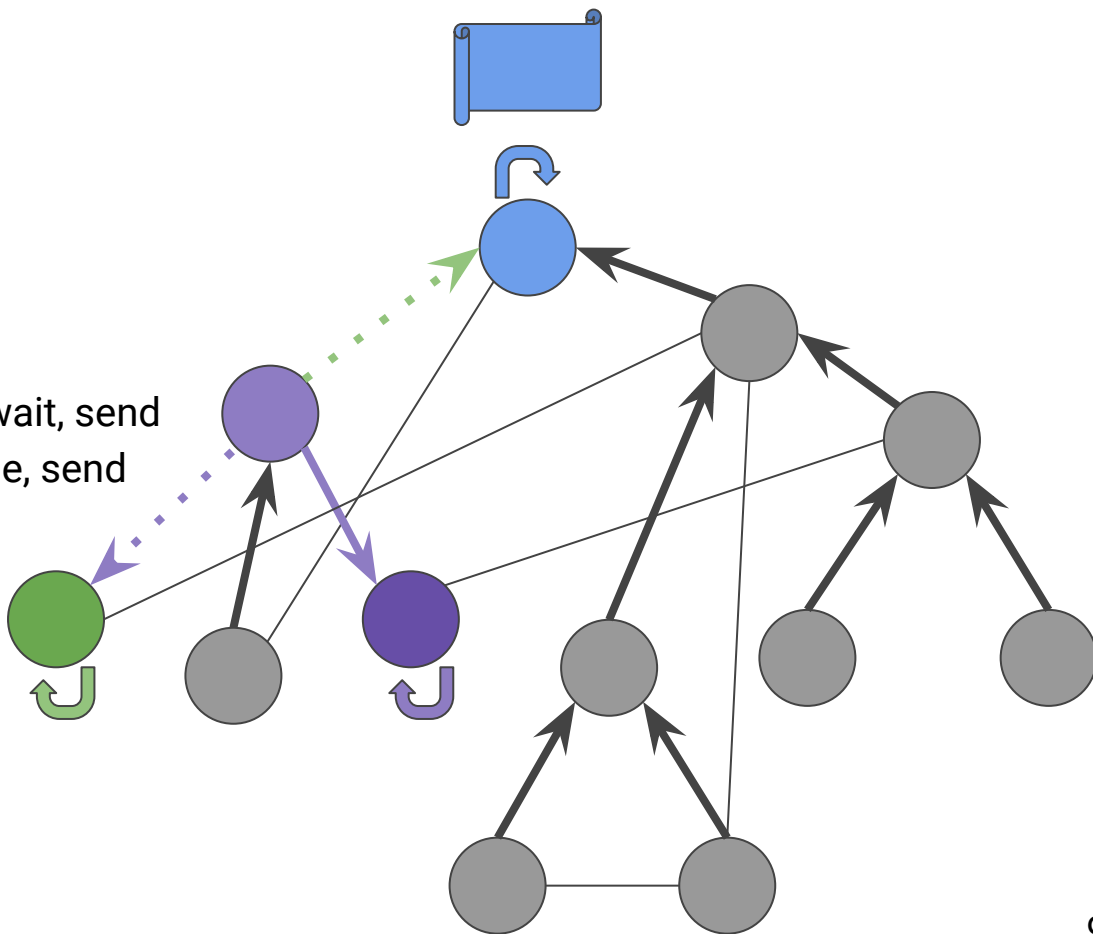
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- Directing tree towards root:
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  - Arrival: reverse arrival edge, send
  - Root: Send, delete self-loop+wait



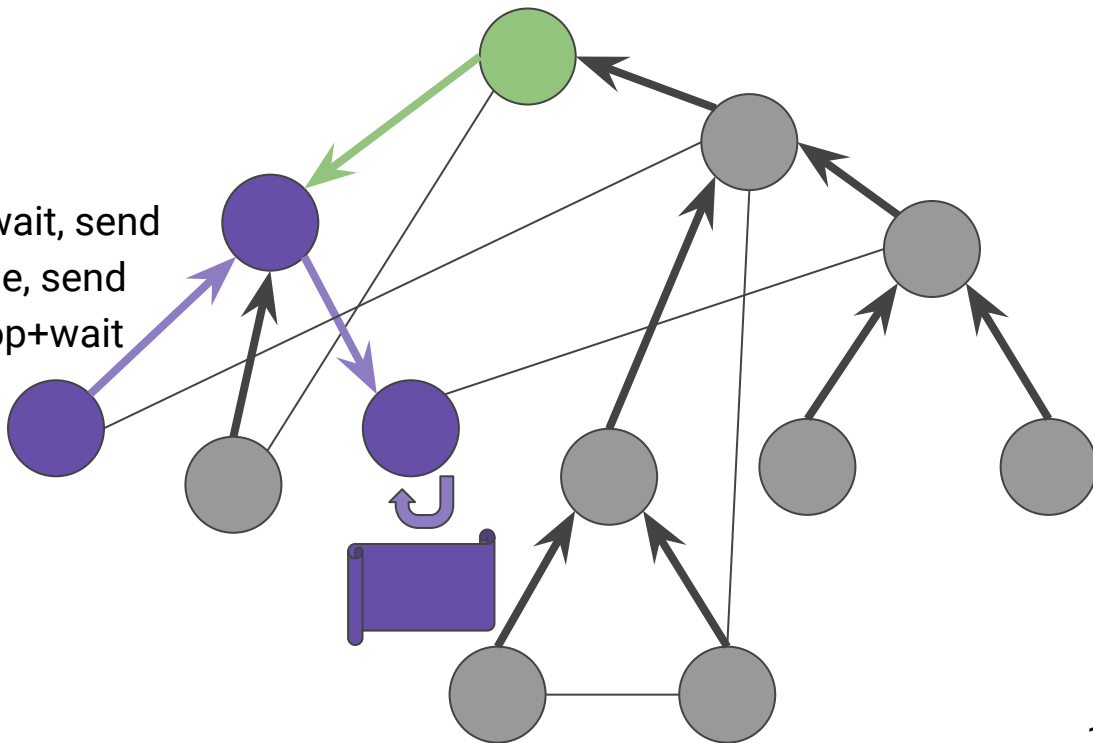
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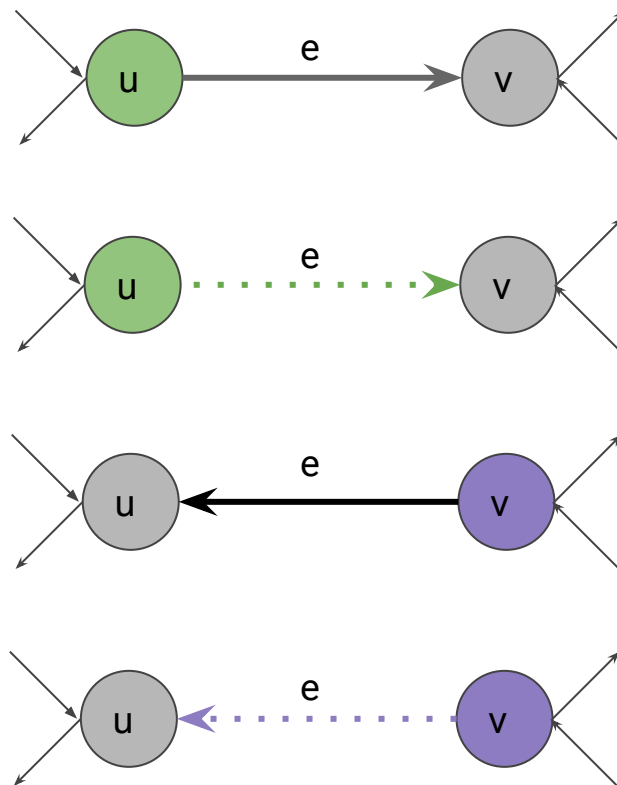
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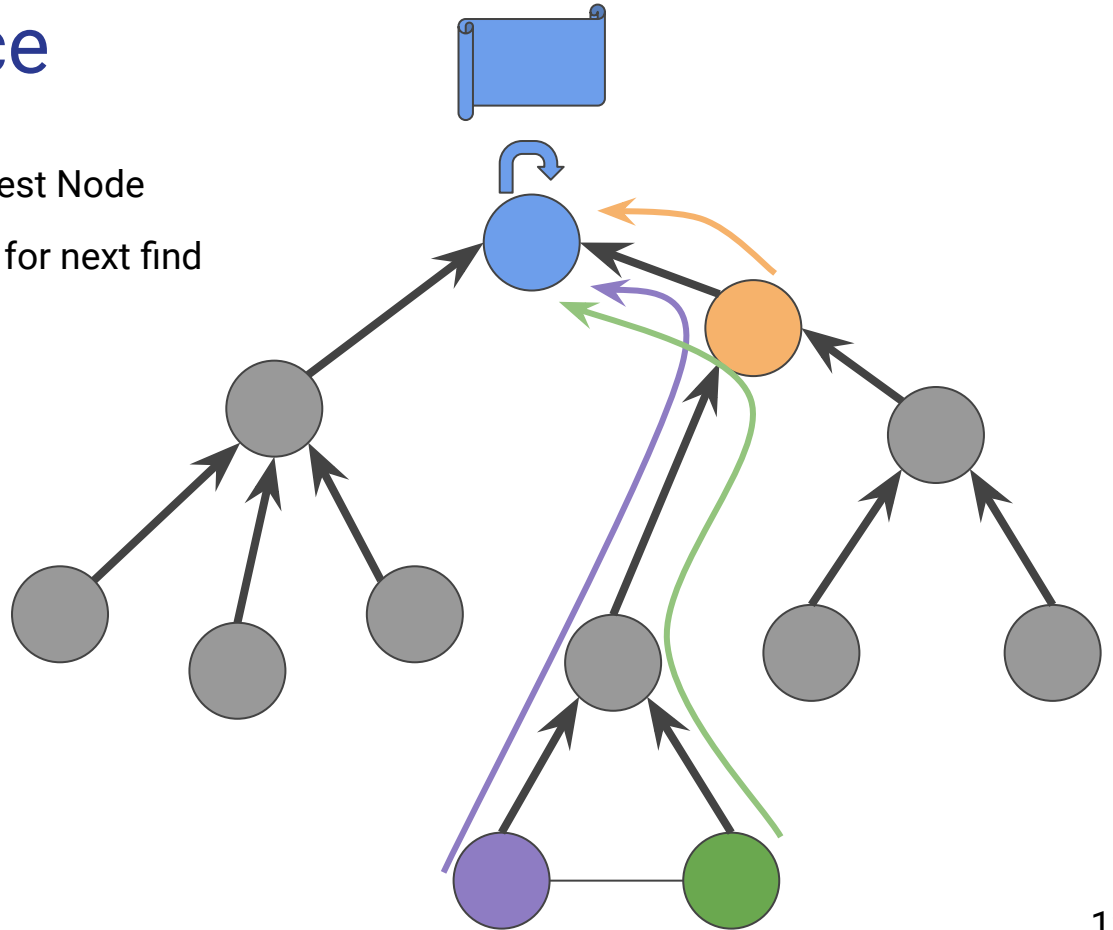
# Arrow: Correctness

- Each edge in just one of the four states
- “Find” requests will go through static tree
- If an edge “e” be traversed twice:
  - Two traversals must be subsequent,
  - But at the end of state “2”, find request will go out of “v”, since each node has always have an outgoing edge



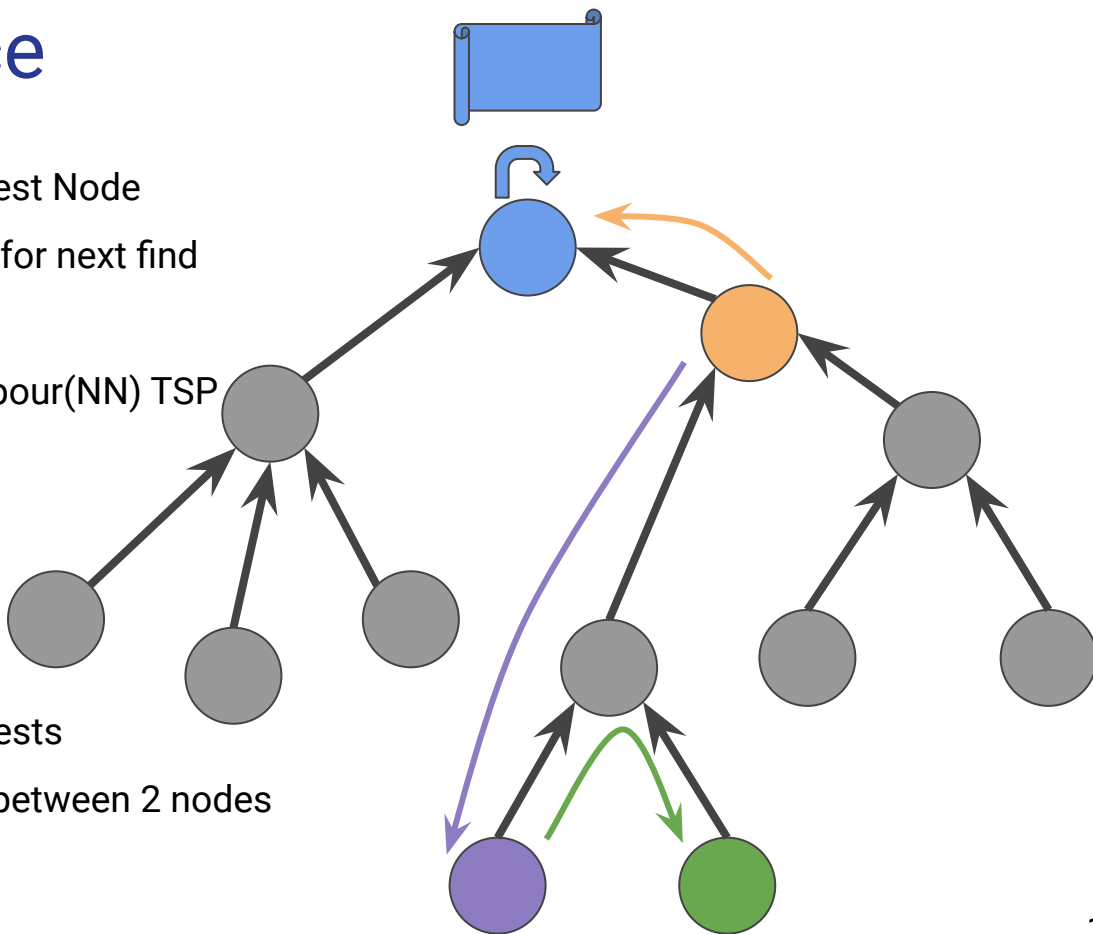
# Arrow: Performance

- First "Find" reaches root  $\leftrightarrow$  Nearest Node
- Everything "seems" to be reseted for next find



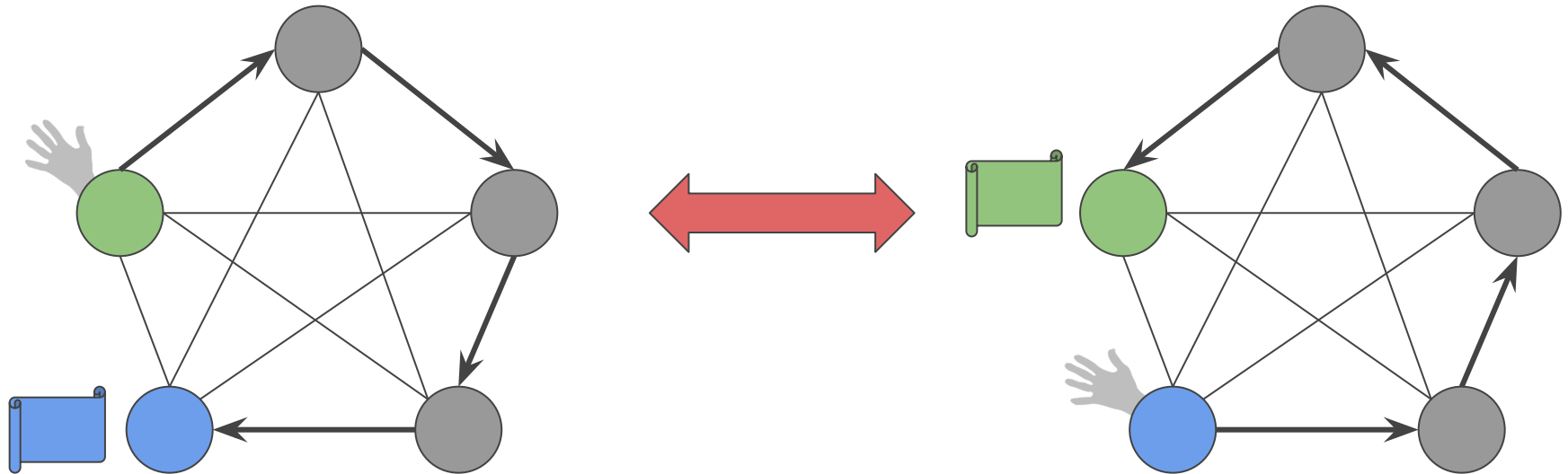
# Arrow: Performance

- First “Find” reaches root  $\leftrightarrow$  Nearest Node
- Everything “seems” to be reseted for next find
- Algorithm mimics Nearest Neighbour(NN) TSP
- $C_{NN} \leq \frac{3}{2} \lceil \log_2 D \rceil C_{Optimal}$
- Ordering Cost:
  - For “find” operations
  - latency?  $\rightarrow$  Well-space requests
  - |messages|?  $\rightarrow$  Alternating between 2 nodes
  - latency + |messages|



# Arrow: Bad example

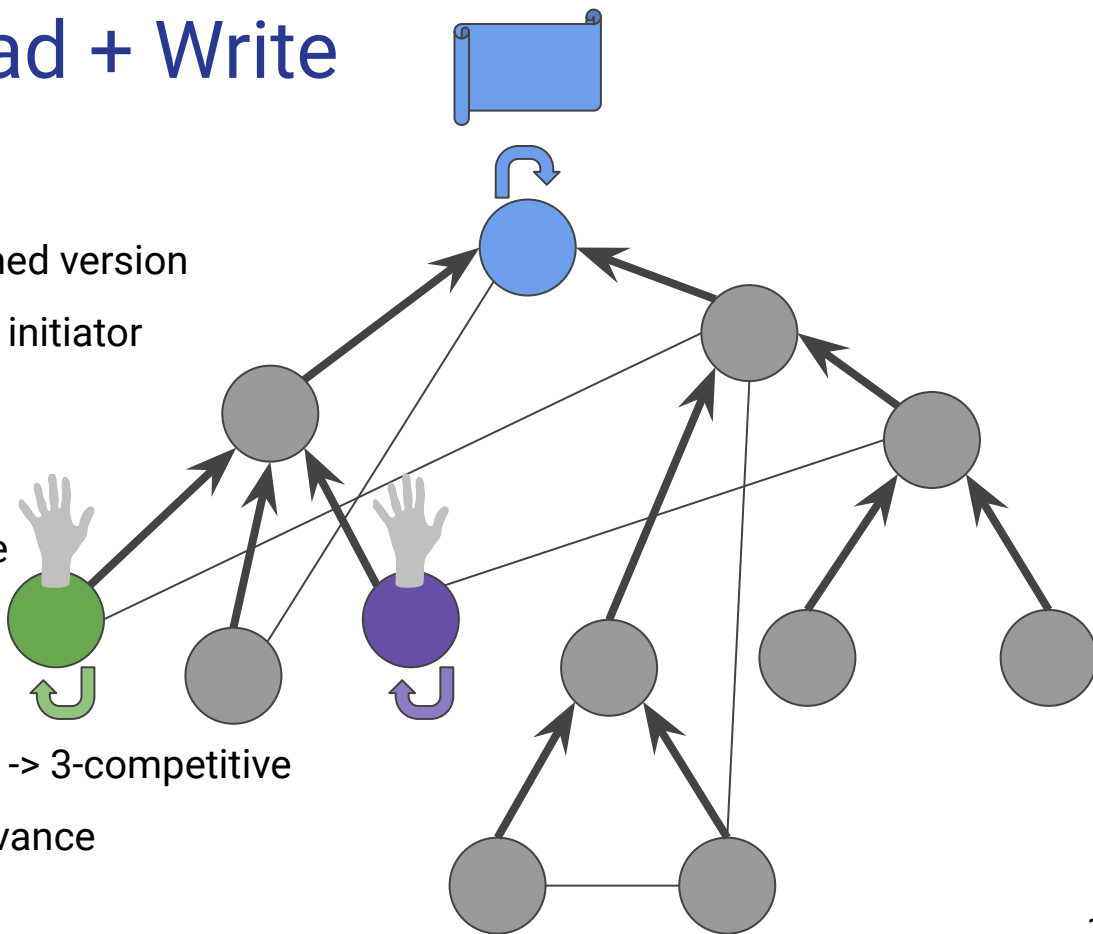
- Dependent on the choice of spanning tree
- Lack of auto-adjustments





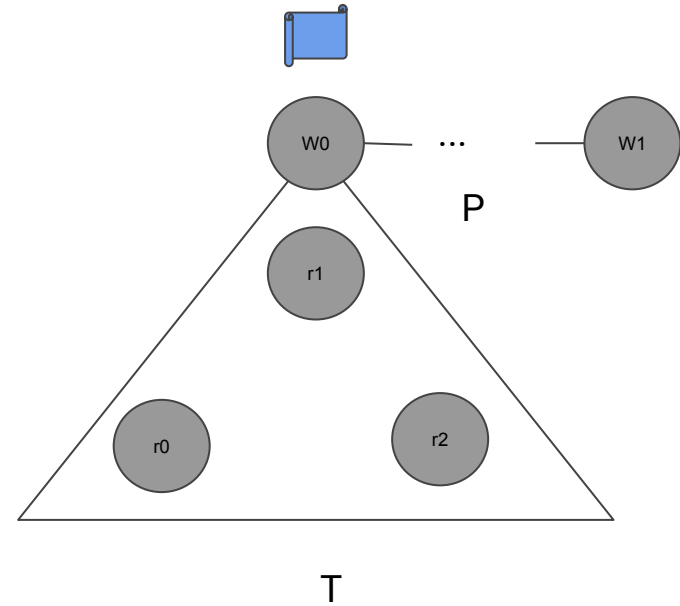
# Arrow: Multiple Read + Write

- Read:
  - Follow arrows until a cached version
  - Cache on the way back to initiator
- Write:
  - Change the value locally
  - Follow arrows and reverse
  - Flag cached as obsolete
- Performance:
  - Only message complexity -> 3-competitive
  - Time -> Opt cach all in advance



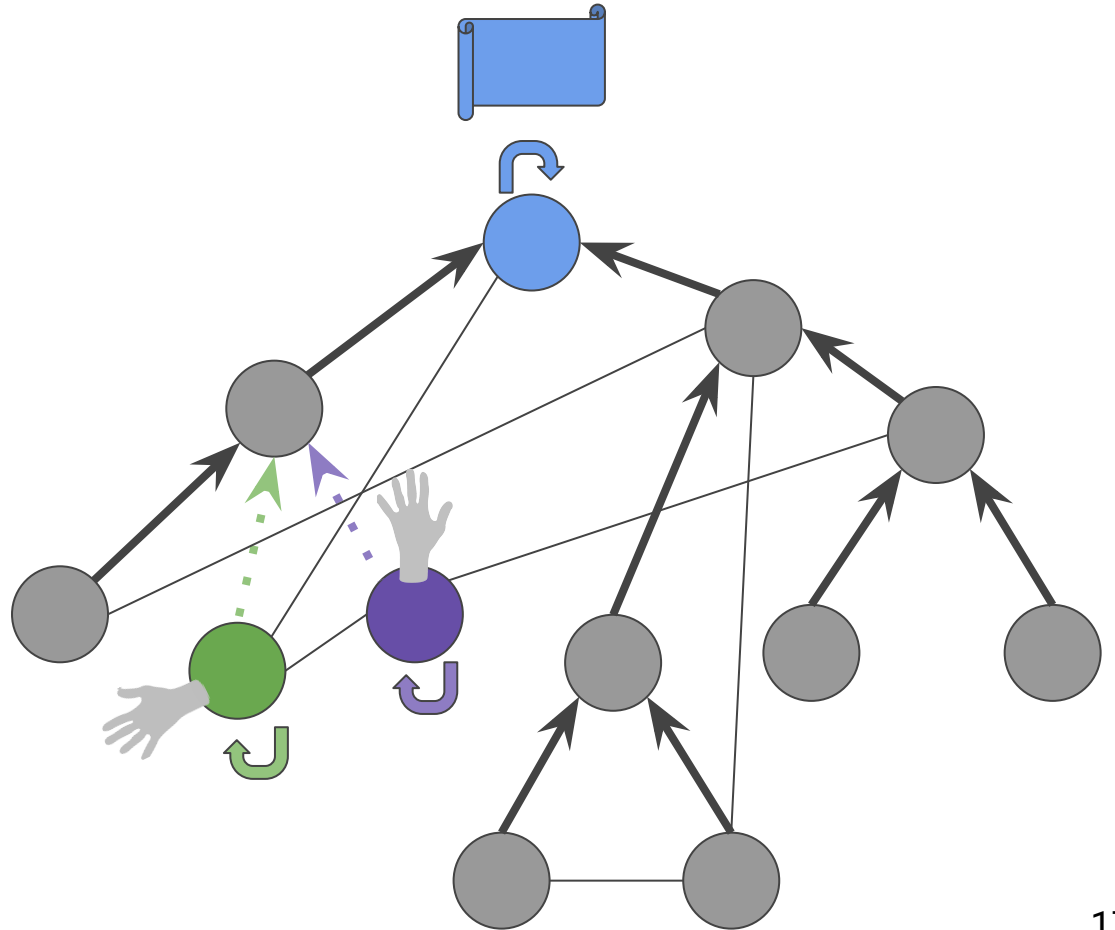
# Arrow: 3-competitiveness

- $w_0, r_0, r_1, \dots, w_1$
- Alg :
  - Read  $\rightarrow 2|T|$
  - Write  $\rightarrow |T|+|P|$
- OPT:
  - $|T|+|P|$



# Ivy: Protocol

- Assume complete graph
- Start as Arrow



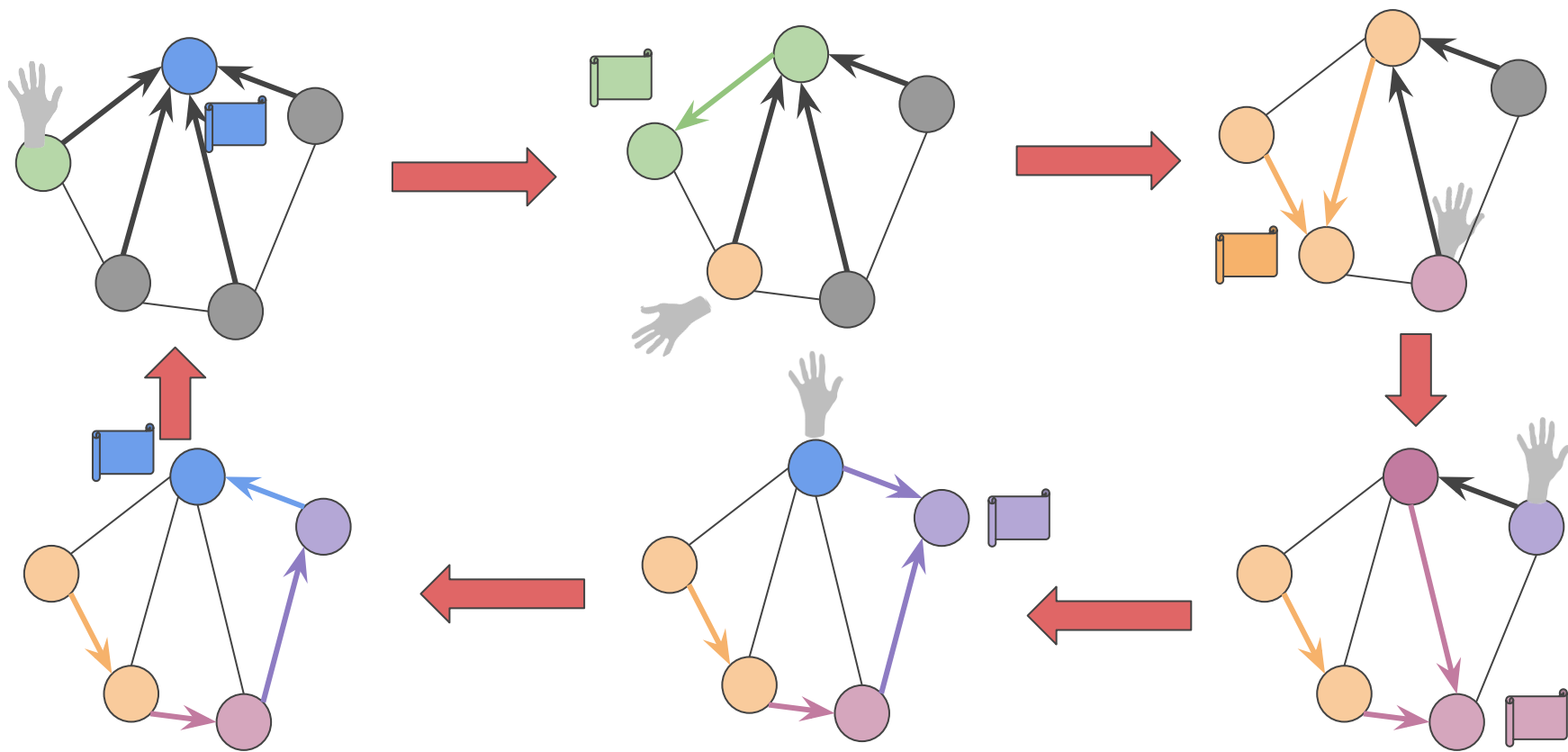








# Ivy: Bad example





# Ivy: Analysis

$$\Phi(T) = \sum_{u \in V} \frac{\log s(u)}{2}.$$

$$a_i = k_i - \Phi(T_{i-1}) + \Phi(T_i)$$

Cost of "i"th request

$$1 + \log(\alpha - 1)/2 \leq \log \alpha$$

$$a_i = k_i + \frac{1}{2} \cdot \sum_{j=0}^{k_i-1} \log \left( \frac{s_{j+1} - s_j}{s_j} \right)$$

$$a_i \leq \sum_{j=0}^{k_i-1} \log \frac{s_{j+1}}{s_j}$$

Size of "j"th subtree

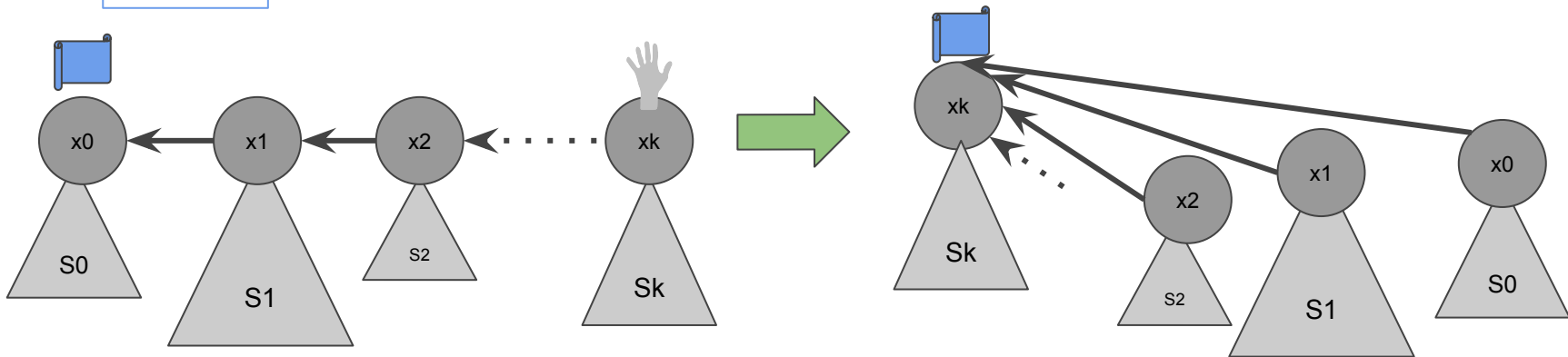
$$= \log s_{k_i} - \log s_0 \leq \log n,$$



$$\sum_{i=1}^m a_i \geq \sum_{i=1}^m k_i.$$

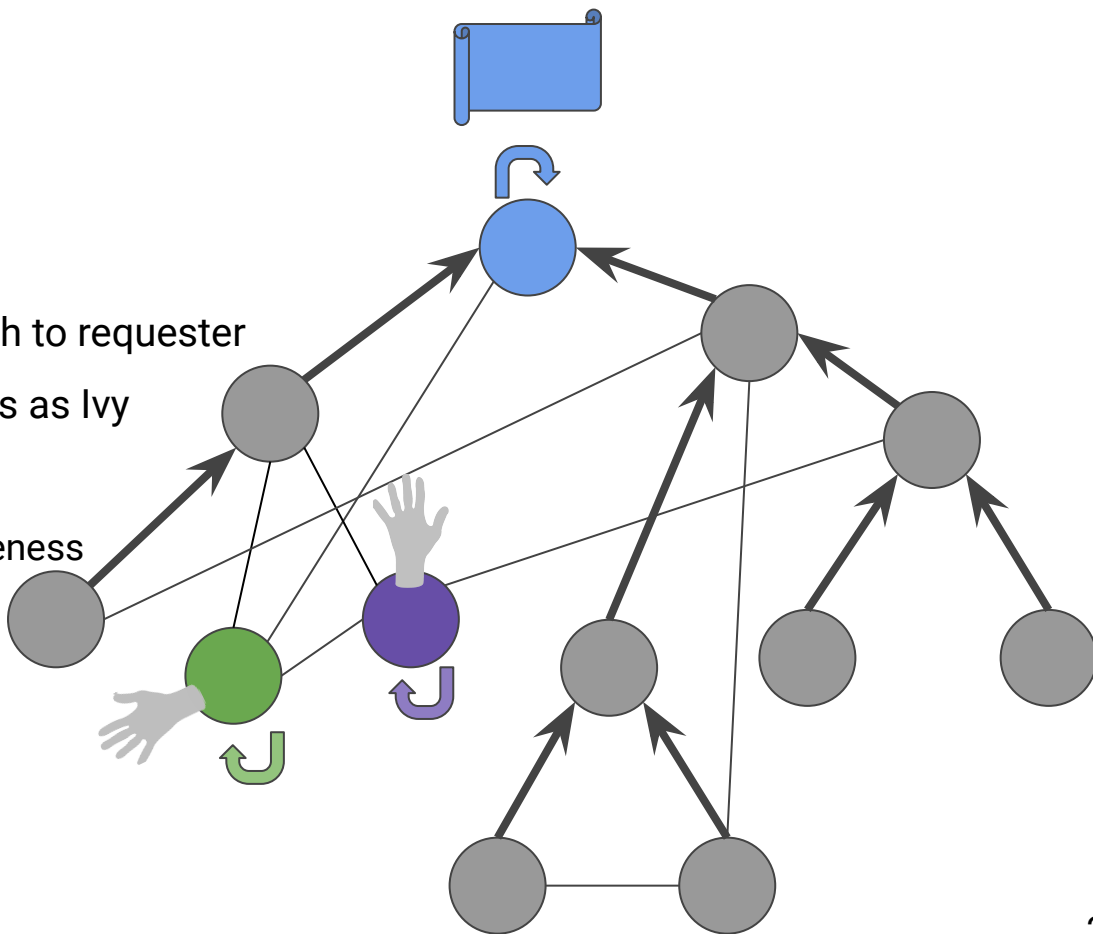


$$\sum_{i=1}^m k_i \leq m \log n$$



# Arvy

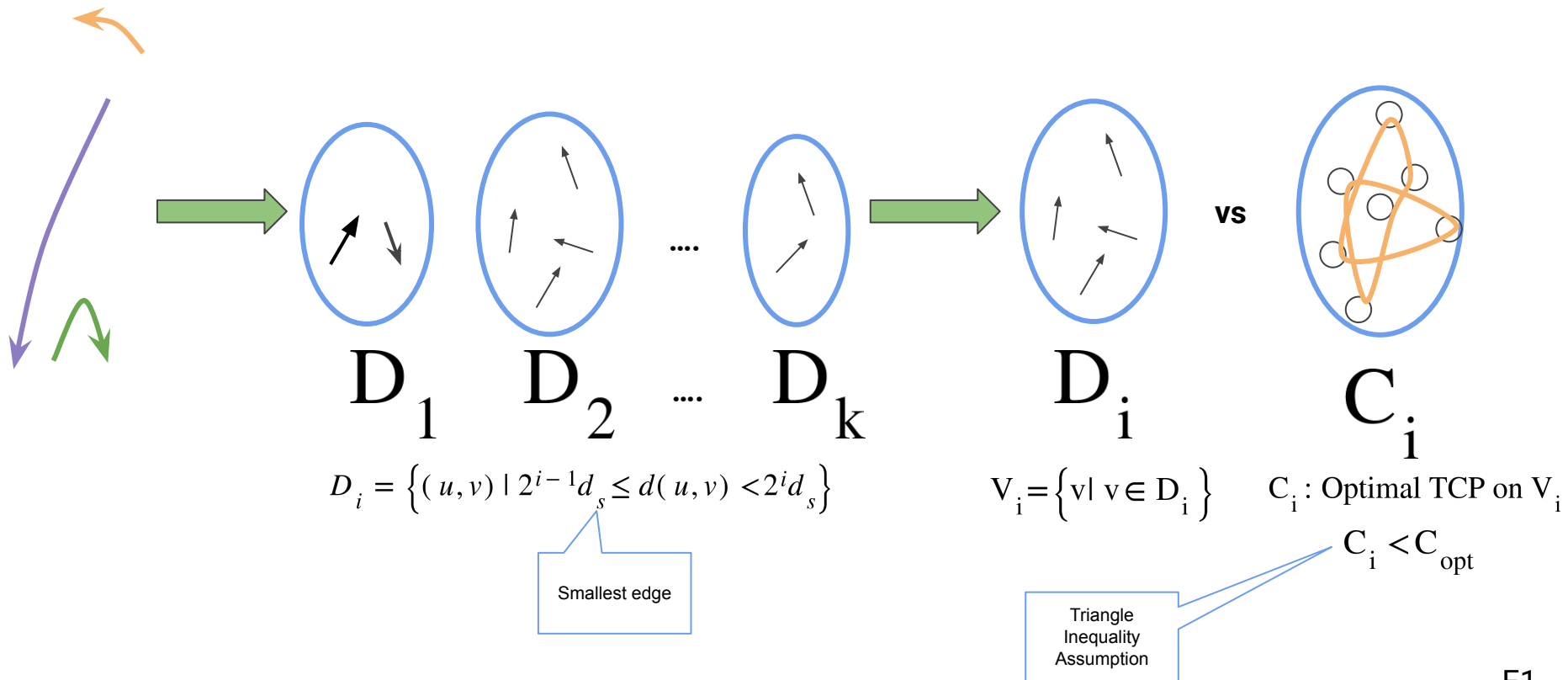
- Start as Arrow
- On arrival:
  - Point to a node on the path to requester
- Same bad example and analysis as Ivy
- On ring:
  - Using bridges 5-competitiveness



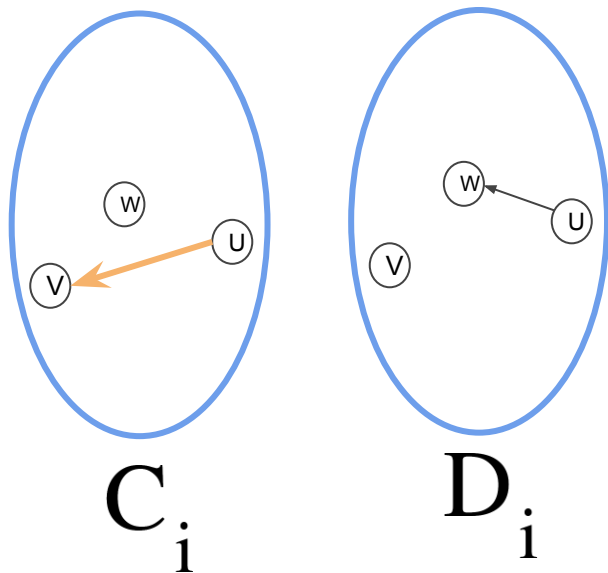
Thank you



# Arrow: Nearest Neighbour TSP



# Arrow: Nearest Neighbour TSP



$$\forall (u, w) \in D_i : d(u, w) \leq 2ds_i$$



$$\sum_{e \in D_i} d(e) \leq \frac{3}{2} \sum_{e \in C_i} d(e)$$



$$\forall (u, v) \in C_i \exists (u, w) \in D_i . d(u, w) < d(u, v)$$